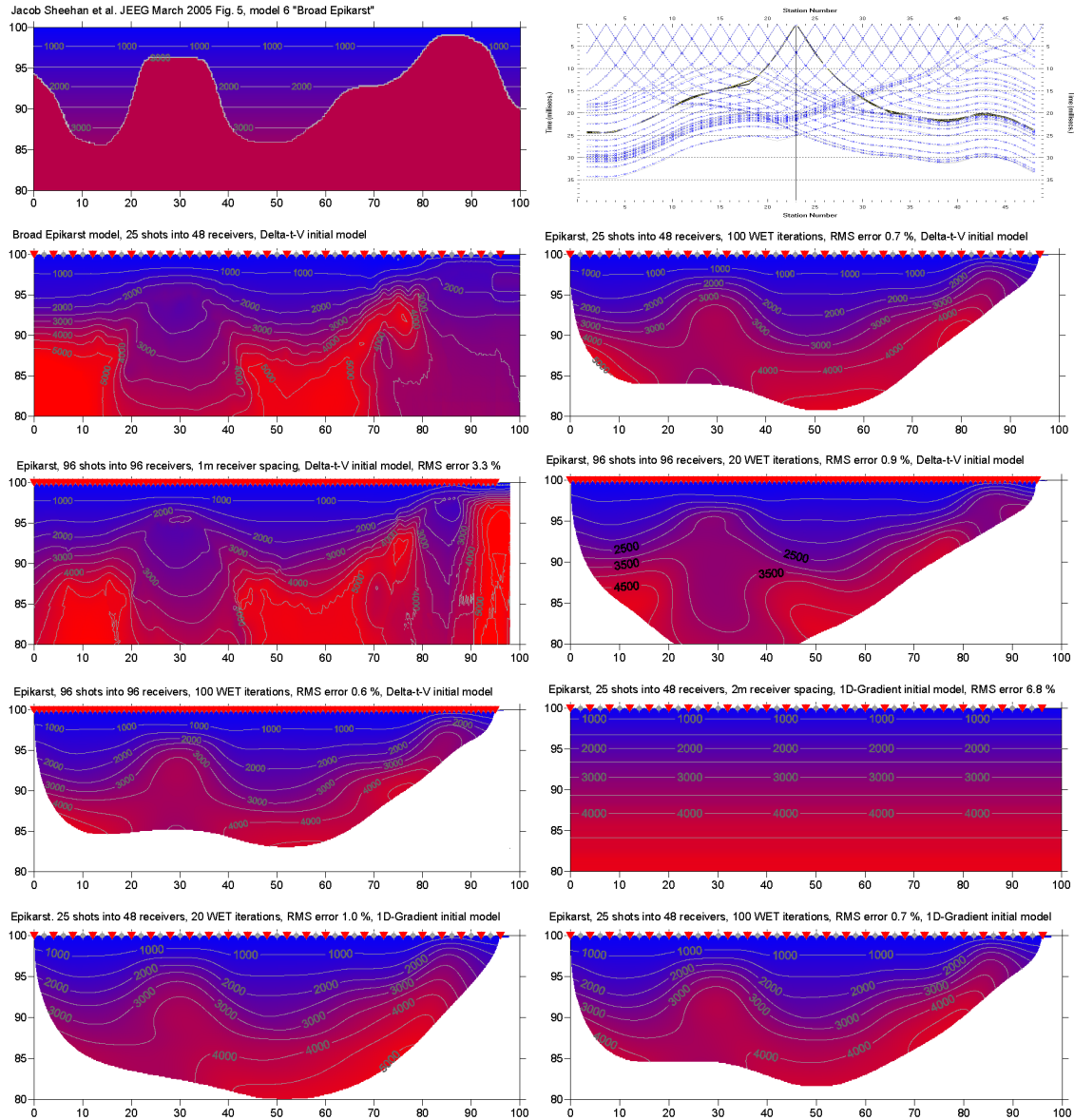


## Interpretation of Sheehan Broad Epikarst Model, with Rayfract® 3.18 and 4.01+WDVS

We show interpretation of the [broad epikarst model](#) described by [Jacob Sheehan](#) in his [JEEG March 2005 evaluation](#). We increase the number of shots, decreasing the shot spacing : shoot at every vs. at every 2<sup>nd</sup> receiver. Also, we decrease the receiver spacing from 2m to 1m. We refine the Delta-t-V pseudo-2D initial model with [WET tomography](#), showing 20 and 100 WET iterations. Finally, we use our default [Smooth inversion](#) method, based on a 1D-Gradient initial model and 20 vs. 100 WET iterations.



Above Delta-t-V interpretation does not improve much with more narrow spacing of shots and receivers. But default Smooth inversion with 1D-gradient initial model (at bottom) works reliably, with just 20 or with 100 WET iterations. Resolution of WET and seismic refraction tomography decreases with increasing imaged depth. See [D.J. White 1989](#), [J.G. Hagedoorn 1959 Fig. 1](#), <http://rayfract.com/tutorials/thrust.pdf> and <http://rayfract.com/tutorials/fig9inv.pdf>.

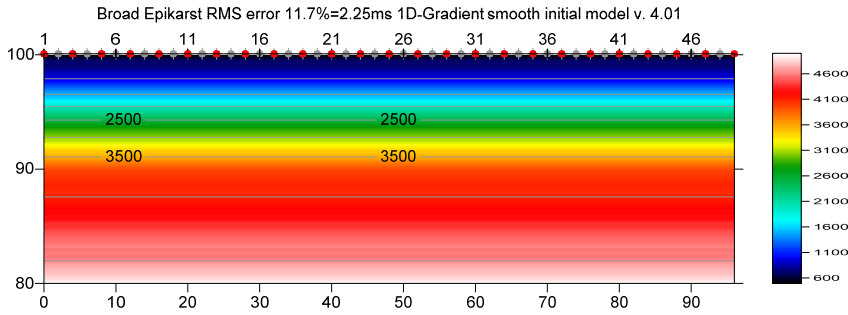


Fig. 1 : 1D-Gradient starting model obtained with Smooth invert|WET with 1D-gradient starting model. Layered XTV enabled in Smooth invert|Smooth inversion Settings. Grid cell size forced to 0.2m in Header|Profile.

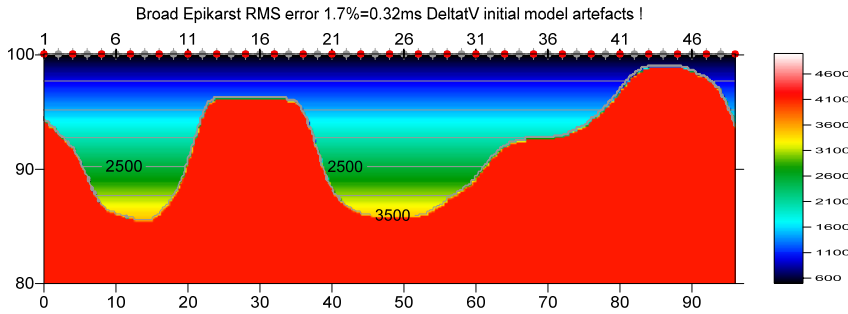


Fig. 2 : true synthetic model made available by Jacob Sheehan in 2005.

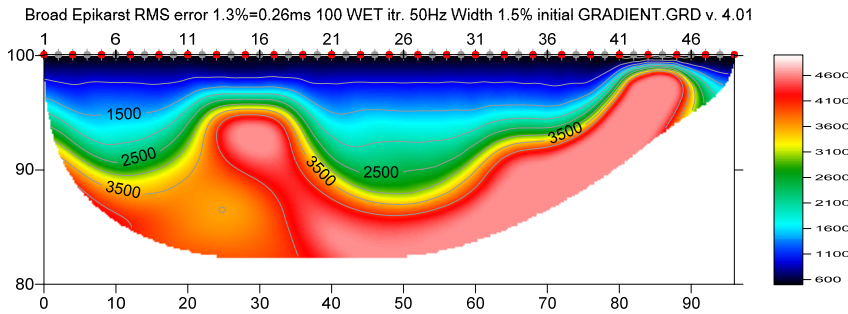


Fig. 3 : 100 Steepest-Descent WET iterations, minimal smoothing, wavepath width halved to 1.5%. Starting model Fig. 1. Wavepath frequency 50Hz. Ricker differentiation -2. Max. WET velocity 4,500 m/s. Don't smooth velocity update. Don't smooth last iteration (Fig. 5). WDVS frequency 400Hz. Angle increment 10 degrees. Regard nth node = 5 (Fig. 6).

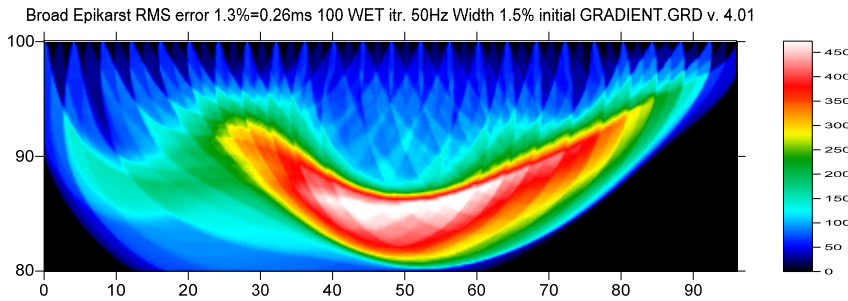


Fig. 4 : WET wavepath coverage plot obtained with Fig. 3. Unit is wavepaths per pixel.

WDVS Wavelength-Dependent Velocity Smoothing is described in [Zelt, C. A. and J. Chen, Frequency-dependent travelt ime tomography for near-surface seismic refraction data, Geophys. J. Int., 207, 72-88, 2016.](#)

Narrowing the wavepath width from default 3% to 1.5% corresponds to increasing the WET frequency. Enabling WDVS and lowering the wavepath width gives higher resolution in overburden but also results in more artefacts in the basement : too high velocity in higher-coverage basement areas, too low velocity in

lower-coverage basement areas (Fig. 3 & Fig. 4). We suppress a WDVS bias towards too high basement velocities by limiting the *max. WET velocity* to 4,500 m/s in *WET Tomo|Interactive WET* (Fig. 5).

**Edit WET Wavepath Eikonal Traveltime Tomography Parameters**

Specify initial velocity model  
 D:\ray32\broadepi\GRADTOMO\GRADIENT.GRD

Stop WET inversion after  
 Number of WET tomography iterations :  iterations  
☐ or RMS error gets below  percent  
☒ or RMS error does not improve for n =  iterations  
☐ or WET inversion runs longer than  minutes

WET regularization settings  
 Wavepath frequency :  Hz   
 Ricker differentiation [-1:Gaussian,-2:Cosine] :  times  
 Wavepath width [percent of one period] :  percent   
 Wavepath envelope width [% of period] :  percent  
 Min. velocity :  Max velocity :  m/sec.  
 Width of Gaussian for one period [sigma] :  sigma

Gradient search method  
☒ Steepest Descent ☐ Conjugate Gradient

Conjugate Gradient Parameters  
 CG iterations  Line Search iters.   
 Tolerance  Line Search tol.   
 Initial step  ☐ Steepest Descent step

**Edit WET Tomography Velocity Smoothing Parameters**

Determination of smoothing filter dimensions  
☐ Full smoothing after each tomography iteration  
☒ Minimal smoothing after each tomography iteration  
☐ Manual specification of smoothing filter, see below

Smoothing filter dimensions  
 Half smoothing filter width :  columns  
 Half smoothing filter height :  grid rows

Suppress artefacts below steep topography  
☒ Adapt shape of filter. Uncheck for better resolution.

Maximum relative velocity update after each iteration  
 Maximum velocity update :  percent

Smooth after each nth iteration only  
 Smooth nth iteration : n =  iterations

Smoothing filter weighting  
☐ Gaussian ☒ Uniform ☐ No smoothing  
 Used width of Gaussian  sigma  
 Uniform central row weight  [1..100]

Smooth velocity update before updating tomogram  
☐ Smooth update ☐ Smooth nth ☐ Smooth last

Damping of tomogram with previous iteration tomogram  
 Damping [0..1]  ☐ Damp before smoothing

Fig. 5 : WET Tomo|Interactive WET tomography (left). Edit velocity smoothing (right).

**Edit WDVS (Zelt & Chen 2016)**

Edit parameters for wavelength-dependent velocity smoothing  
☒ use WDVS for forward modeling of traveltimes

WDVS frequency  [Hz]  
 Angle increment  [Degree]  
 Regard nth node  [node]

Parameters for Cosine-Squared weighting function  
 a : Cosine argument power  [power]  
 b : Cosine-Squared power  [power]

Fig. 6 : Model|WDVS Smoothing

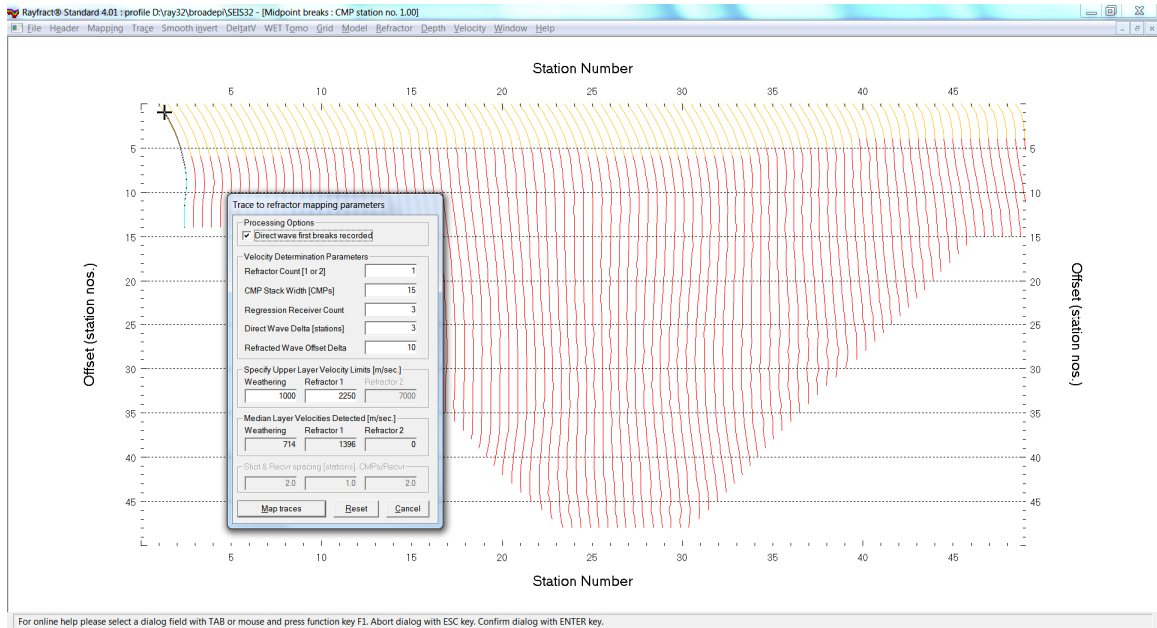


Fig. 7 : Map first breaks to refractors in Refractor|Midpoint breaks. Press ALT+M and edit 1D velocity model. Click Map traces. Press ALT+G and press ENTER to laterally smooth crossover distances.

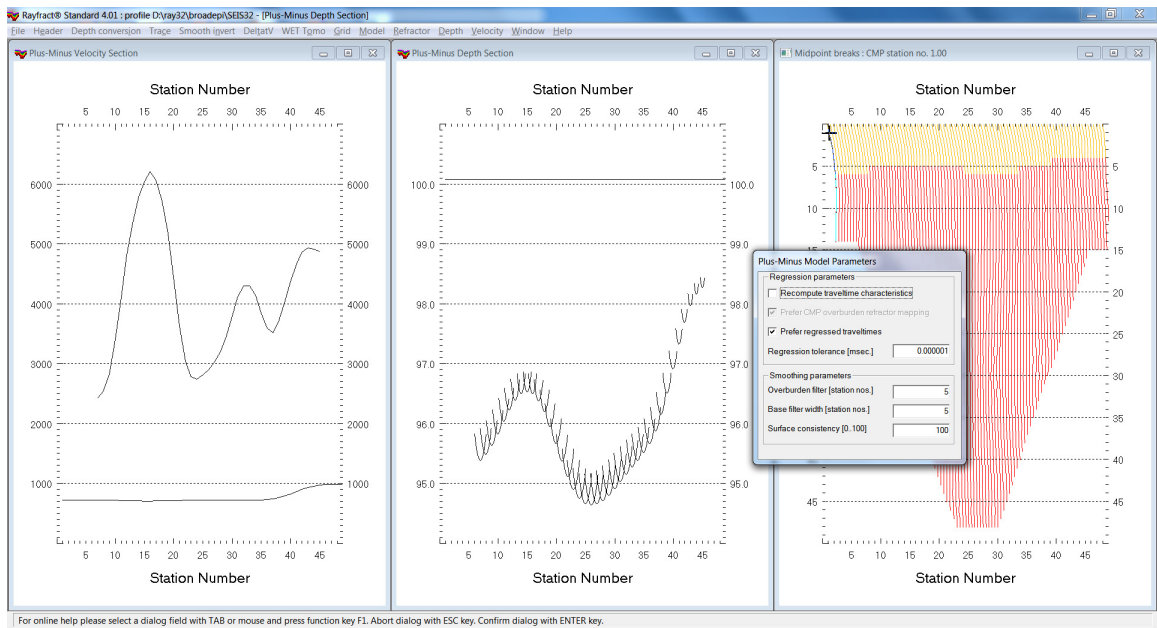


Fig. 8 : select Depth|Plus-Minus. When asked to continue with WET click No button. Press ALT+M to edit lateral refractor smoothing : decrease Base filter width from 10 station nos. to 5. Press ENTER to redisplay Plus-Minus starting model in Surfer (Fig. 9). When prompted to continue with WET click Yes button to obtain Fig. 10 and Fig. 11.

For typical field surveys with [reciprocal traveltimes picking errors](#) and errors in recording geometry specification we recommend to increase the default WET wavepath width instead e.g. multiply by two. See our tutorial <http://rayfract.com/tutorials/Aaknes-1.pdf>.

When enabling WDV as shown above we can minimize WET smoothing more than without WDV. This results in sharper imaging of layer boundaries and increased resolution in the WET tomogram.

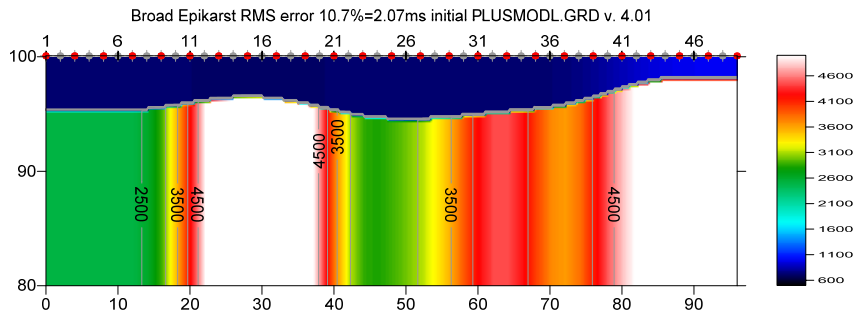


Fig. 9 : Plus-Minus method starting model obtained as in Fig. 8.  
Broad Epikarst RMS error 2.7%=0.52ms 20 WET itr. 50Hz Width 3.0% initial PLUSMODL.GRD v. 4.01

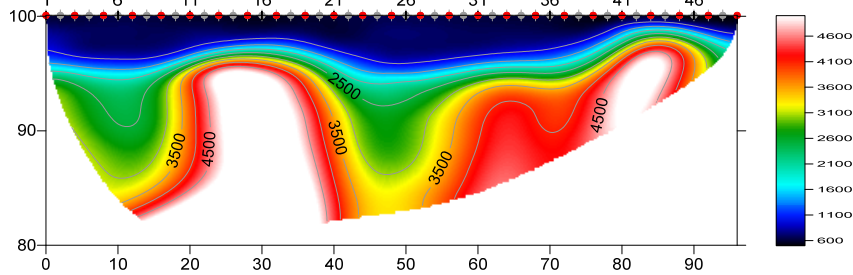


Fig. 10 : Smooth inversion with Plus-Minus starting model (Fig. 9). WDVS enabled (Fig. 6.).  
Broad Epikarst RMS error 2.7%=0.52ms 20 WET itr. 50Hz Width 3.0% initial PLUSMODL.GRD v. 4.01

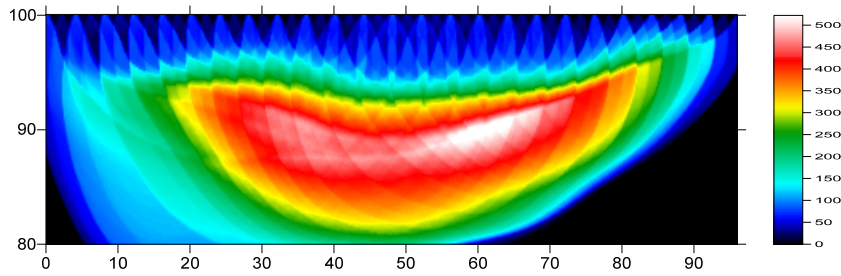


Fig. 11 : WET wavepath coverage plot obtained with Fig. 10. Unit is wavepaths per pixel.  
Broad Epikarst RMS error 1.6%=0.30ms 100 WET itr. 50Hz Width 1.5% initial PLUSMODL.GRD v. 4.01

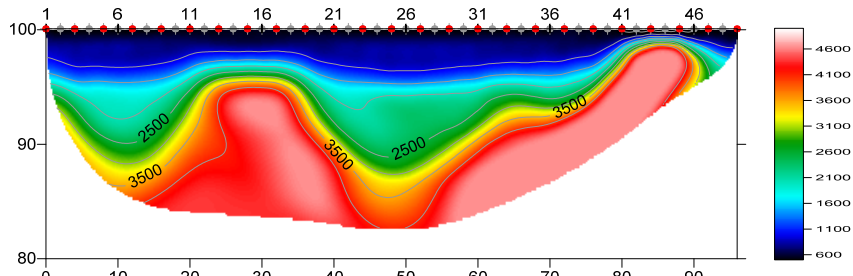


Fig. 12 : 100 Steepest-Descent WET iterations, minimal smoothing (Fig. 5). Starting model Fig. 9. WDVS frequency 400Hz (Fig. 6). Compare with Fig. 3 obtained with 1D-gradient starting model (Fig. 1).

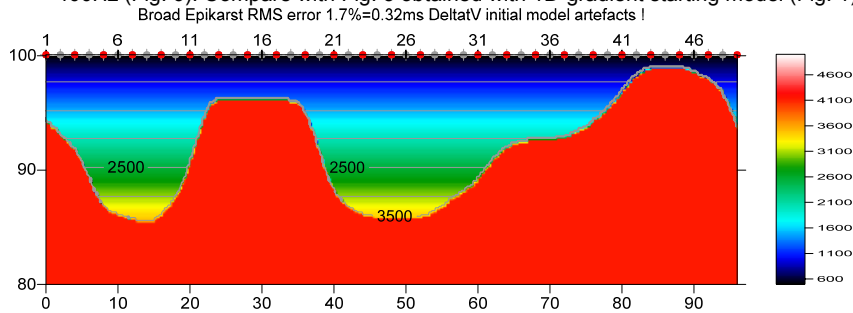


Fig. 13 : true synthetic model made available by Jacob Sheehan in 2005.

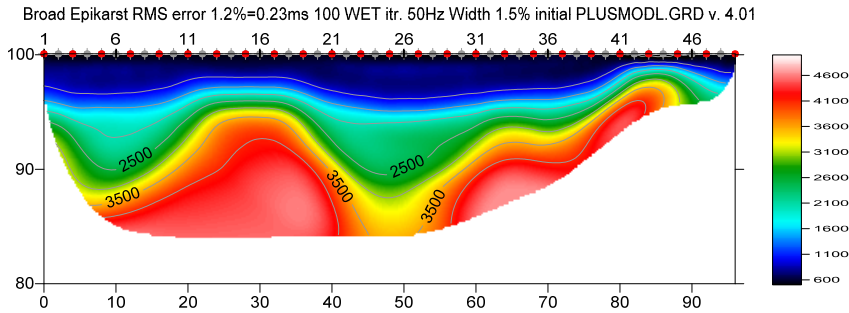


Fig. 14 : 100 Steepest-Descent WET iterations, minimal smoothing (Fig. 5). Starting model Fig. 9. WDVS disabled. Compare with Fig. 12 obtained with same WET settings and same starting model but with WDVS enabled (Fig. 6).

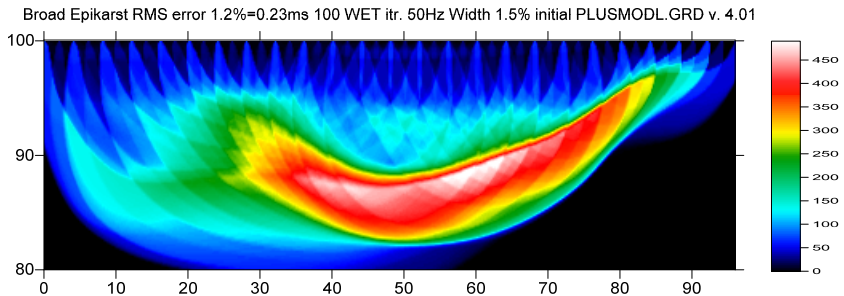


Fig. 15 : WET wavepath coverage plot obtained with Fig. 14. Unit is wavepaths per pixel.

In Fig. 7 and Fig. 8 we show mapping of traces to refractors and layered refraction interpretation with Plus-Minus method. We obtain the Plus-Minus starting model Fig. 9. Default Smooth inversion using starting model Fig. 9 and 20 Steepest-Descent WET iterations with full WET smoothing gives Fig. 10 and Fig. 11. Interactive WET (Fig. 5) with starting model Fig. 9 gives Fig. 12.

We have shown that WET inversion using 100 Steepest-Descent WET iterations with minimal WET smoothing and WDVS enabled is independent of the starting model and matches the true model.

Also we show 100 Steepest-Descent WET iterations without WDVS and with minimal smoothing and starting model Fig. 9 in Fig. 14. Compare with Fig. 12 showing same WET inversion with WDVS enabled.

Note the anomalously high apparent Plus-Minus velocity at station no. 15 in Fig. 8 and Fig. 9. This shows that Plus-Minus velocity is not always realistic with strong refractor curvature, as is pseudo-2D DeltatV velocity shown on first page.

Decreasing WDVS parameters *Angle increment* from 10 to 5 degrees and *Regard nth node* from 5 to 2 (Fig. 6) helps to slightly increase contrast in Fig. 3 just below topography at station no. 43 but increases WET inversion runtime.

See our updated [help file](#) for description of WDVS parameters in chapter **Forward model traveltimes**. Press F1 function key in **Model|WDVS Smoothing dialog** (Fig. 6) to display popup help window for current control. Use TAB key to switch focus between controls.

Our default [Smooth inversion](#) based on a 1D-Gradient initial model and 20 or 100 WET iterations as detailed in our [SAGEEP 2010 short course](#) (without WDVS or with default WDVS settings) with default DeltatV and WET settings should work fine in most cases, to give a reliable but possibly low-resolution first interpretation.



If you want higher resolution then you will have to invest more time into tuning WET + WDVS settings and [DeltatV settings](#) for 1D-gradient starting model. As a first step increase the number of WET iterations from default 20 Steepest Descent iterations to 100 iterations. Optionally enable WDVS and decrease the WET smoothing for consistently picked traveltimes and with correctly specified recording geometry as shown above.

The higher the targeted resolution, the higher the uncertainty in WET results will be especially with realistic field data with [reciprocal traveltime picking errors](#) and recording geometry specification errors. Again see

<http://rayfract.com/tutorials/Aaknes-1.pdf>

Here is the .RAR archive with version 4.01 profile database for Fig. 3 :

[http://rayfract.com/tutorials/broadepi\\_seis32\\_SDWET\\_Nov6\\_2020.rar](http://rayfract.com/tutorials/broadepi_seis32_SDWET_Nov6_2020.rar)

Here is the .RAR archive with Surfer 11 .GRD and .PAR files and .SRF plots for Fig. 3 and Fig. 4 :

[http://rayfract.com/tutorials/GRADTOMO\\_WDVS\\_Nov6\\_2020.rar](http://rayfract.com/tutorials/GRADTOMO_WDVS_Nov6_2020.rar)

Here is the .RAR archive with version 4.01 profile database for Fig. 9 to Fig. 12 :

[http://rayfract.com/tutorials/broadepi\\_seis32\\_LayrTomo\\_Dec7\\_2020.rar](http://rayfract.com/tutorials/broadepi_seis32_LayrTomo_Dec7_2020.rar)

Here is the .RAR archive with Surfer 11 .GRD and .PAR files and .SRF plots for Fig. 9 to Fig. 12 :

[http://rayfract.com/tutorials/LAYRTOMO\\_WDVS\\_Dec7\\_2020.rar](http://rayfract.com/tutorials/LAYRTOMO_WDVS_Dec7_2020.rar)

Here is the full link to our SAGEEP 2010 short course :

<http://rayfract.com/SAGEEP10.pdf>

Here is the link to Schuster 1993 WET theory paper :

<http://library.seg.org/doi/abs/10.1190/1.1443514>

We thank Jacob Sheehan for making available this crucial [model and synthetic data](#) .

Also we thank Prof. Colin Zelt for describing the [WDVS algorithm](#) .

Edited in Vancouver, Canada on Dec 8, 2020 by Siegfried Rohdewald, Dipl. Informatik-Ing. ETH.

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